Fall 2014

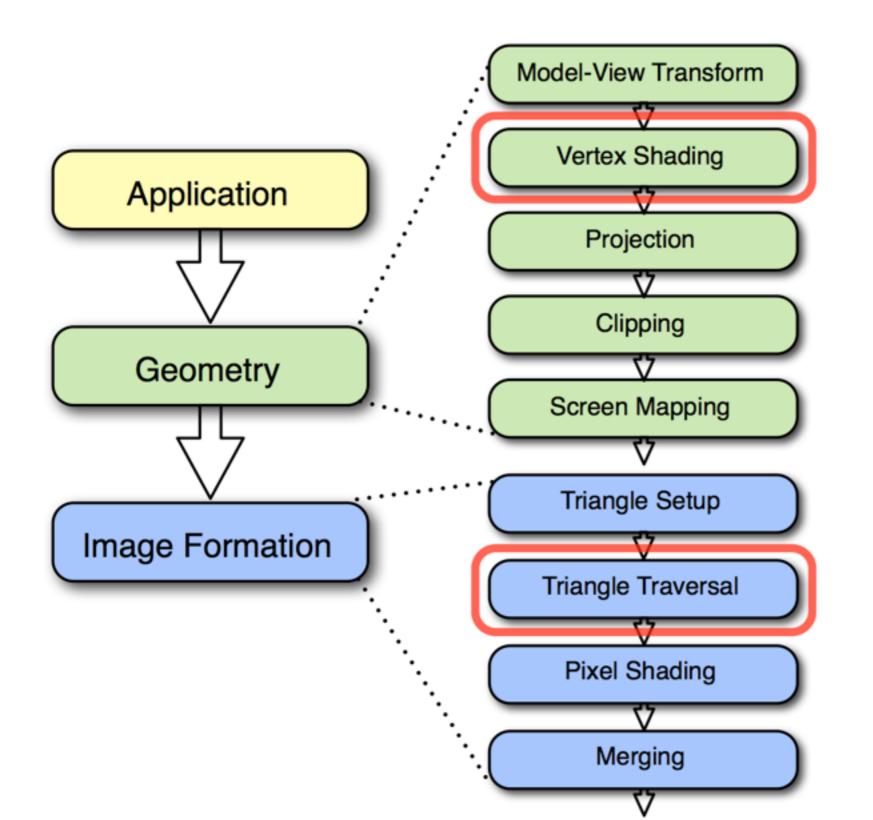
1

CSCI 420: Computer Graphics

# 7.1 Rasterization



# **Rendering Pipeline**



compute vertex attributes, e.g. evaluate lighting model to compute vertex color

rasterize triangles and interpolate vertex attributes

2

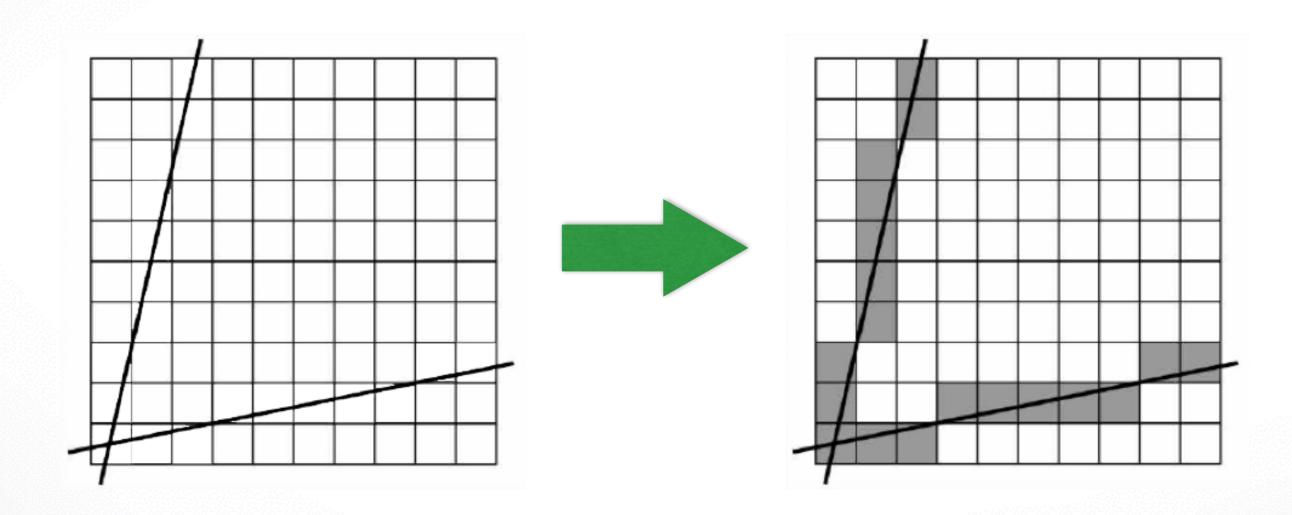
# Outline

- Scan Conversion for Lines
- Scan Conversion for Polygons
- Antialiasing

### **Rasterization (scan conversion)**

- Final step in pipeline: rasterization
- From screen coordinates (float) to pixels (int)
- Writing pixels into frame buffer
- Separate buffers:
  - depth (z-buffer),
  - display (frame buffer),
  - shadows (stencil buffer),
  - blending (accumulation buffer)

# **Rasterizing a line**

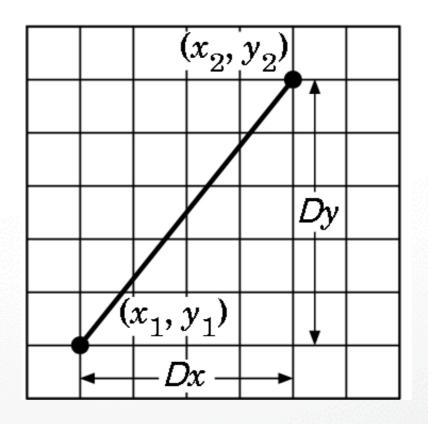


#### **Digital Differential Analyzer (DDA)**

Represent line as

$$y = mx + h$$
 where  $m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{\Delta y}{\Delta x}$ 

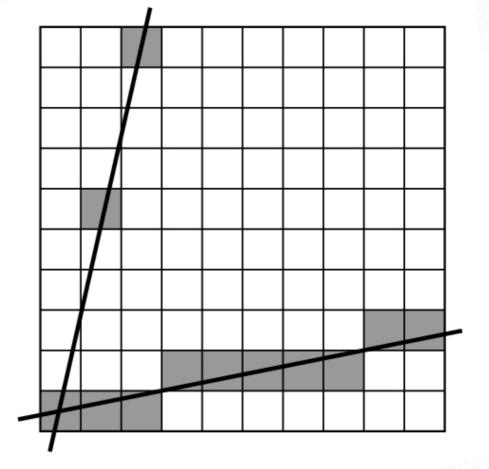
- Then, if  $\Delta x = 1$  pixel, we have  $\Delta y = m \ \Delta x = m$ 



# **Digital Differential Analyzer**

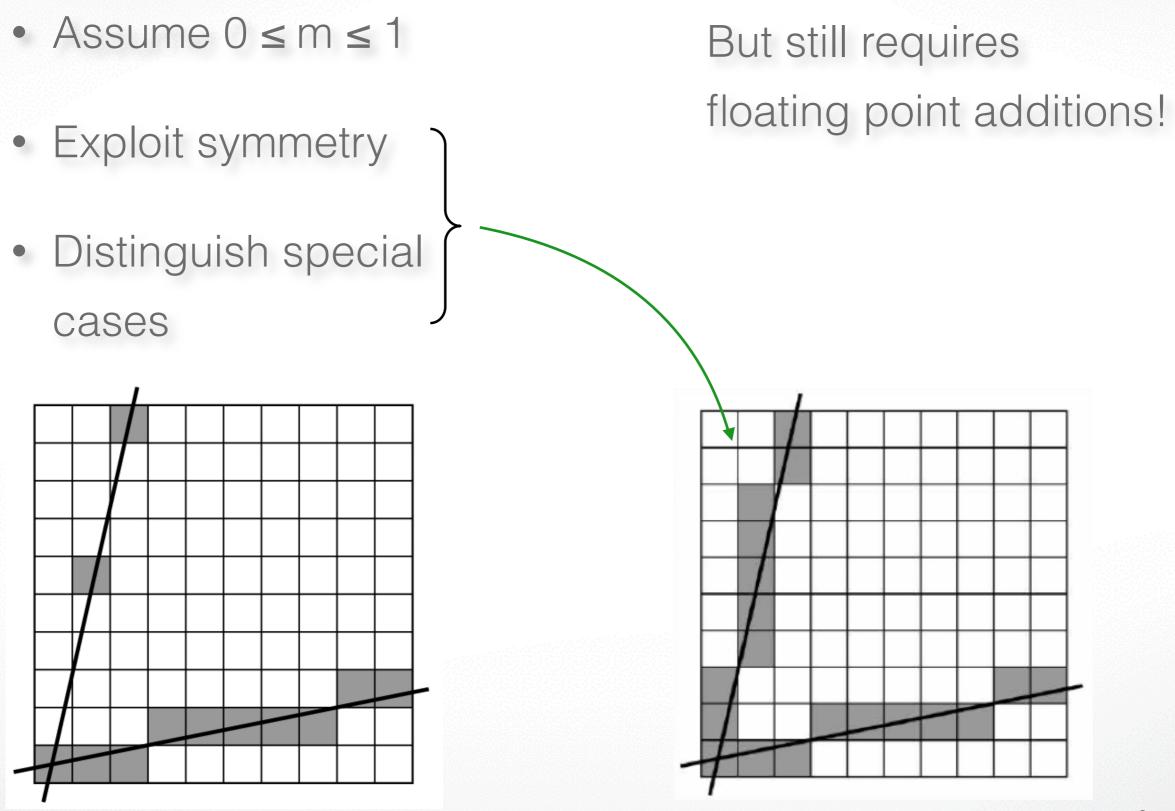
• Assume write\_pixel(int x, int y, int value)

```
for (i = x1; i <= x2; i++)
{
    y += m;
    write_pixel(i, round(y), color);
}</pre>
```



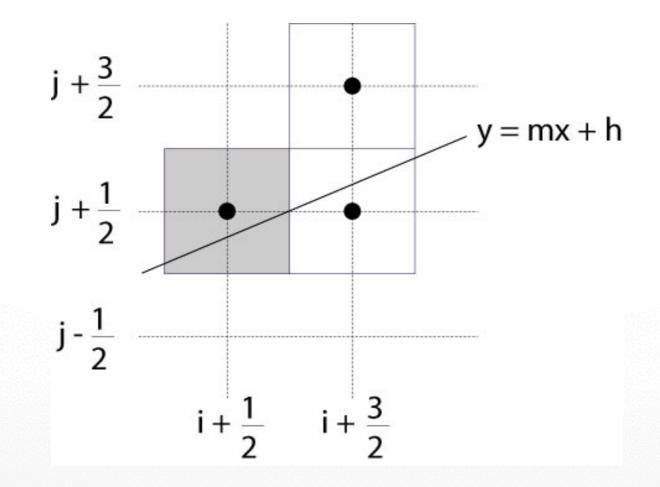
- Problems:
  - Requires floating point addition
  - Missing pixels with steep slopes: slope restriction needed

# **Digital Differential Analyzer (DDA)**



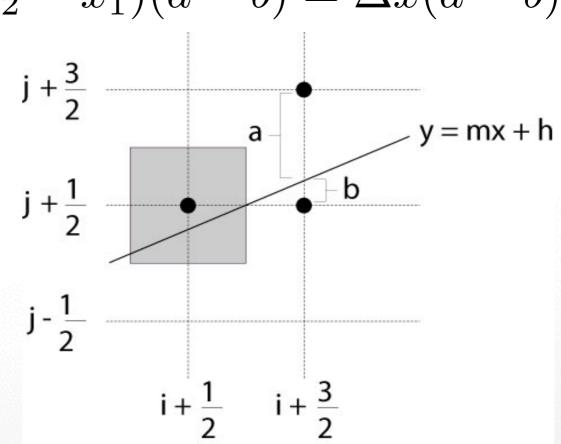
#### **Bresenham's Algorithm I**

- Eliminate floating point addition from DDA
- Assume again  $0 \le m \le 1$
- Assume pixel centers halfway between integers



#### **Bresenham's Algorithm II**

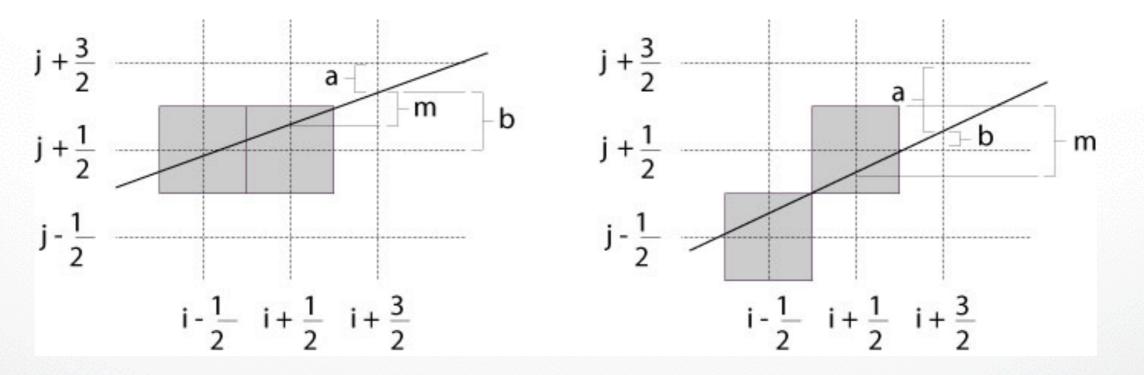
- Decision variable a b
  - If a b > 0 choose lower pixel
  - If  $a b \leq 0$  choose higher pixel
- Goal: avoid explicit computation of a b
- Step 1: re-scale  $d = (x_2 x_1)(a b) = \Delta x(a b)$
- d is always integer



#### **Bresenham's Algorithm III**

- Compute d at step k + 1 from d at step k!
- Case: j did not change  $(d_k > 0)$ - a decreases by m, b increases by m-(a - b) decreases by  $2m = 2(\frac{\Delta y}{\Delta x})$

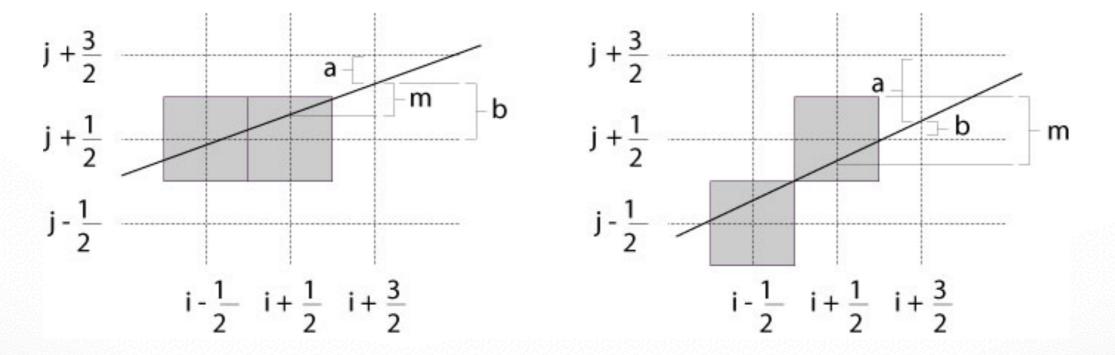
- 
$$\Delta x(a-b)$$
 decreases by  $2\Delta y$ 



#### **Bresenham's Algorithm IV**

- Case: j did change  $(d_k \leq 0)$ 
  - $a\,\mathrm{decreases}\,\,\mathrm{by}\,m-1$  ,  $b\,\,\mathrm{increases}\,\,\mathrm{by}\,m-1$
  - (a-b) decreases by  $2m-2=2(rac{\Delta y}{\Delta x}-1)$

-  $\Delta x(a-b)$  decreases by  $2(\Delta y - \Delta x)$ 



#### **Bresenham's Algorithm V**

• So 
$$d_{k+1} = d_k - 2\Delta y$$
 if  $d_k > 0$ 

• And 
$$d_{k+1} = d_k - 2(\Delta y - \Delta x)$$
 if  $d_k \le 0$ 

• Final (efficient) implementation:

void draw\_line(int x1, int y1, int x2, int y2) {
 int x, y = y0;
 int dx = 2\*(x2-x1), dy = 2\*(y2-y1);
 int dydx = dy-dx, D = (dy-dx)/2;

#### **Bresenham's Algorithm VI**

- Need different cases to handle m > 1
- Highly efficient
- Easy to implement in hardware and software
- Widely used

# Outline

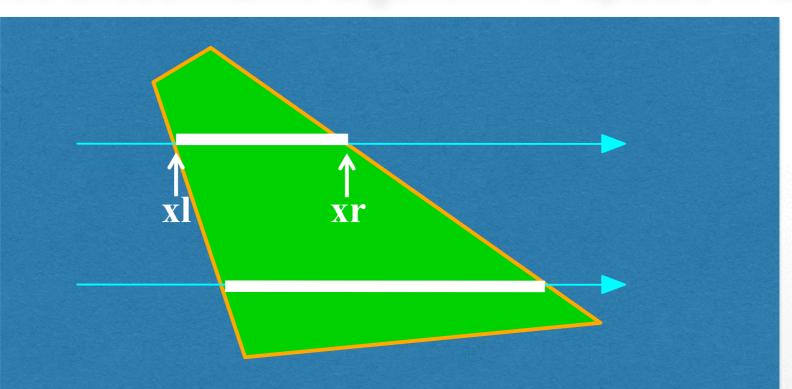
- Scan Conversion for Lines
- Scan Conversion for Polygons
- Antialiasing

### **Scan Conversion of Polygons**

- Multiple tasks:
  - Filling polygon (inside/outside)
  - Pixel shading (color interpolation)
  - Blending (accumulation, not just writing)
  - Depth values (z-buffer hidden-surface removal)
  - Texture coordinate interpolation (texture mapping)
- Hardware efficiency is critical
- Many algorithms for filling (inside/outside)
- Much fewer that handle all tasks well

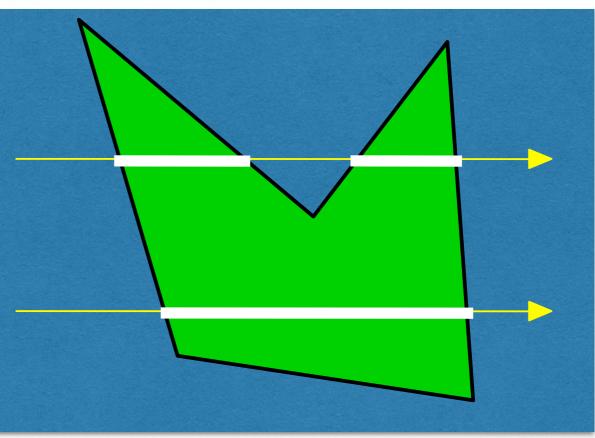
# Filling Convex Polygons

- Find top and bottom vertices
- List edges along left and right sides
- For each scan line from bottom to top
  - Find left and right endpoints of span, xI and xr
  - Fill pixels between xl and xr
  - Can use Bresenham's algorithm to update xI and xr



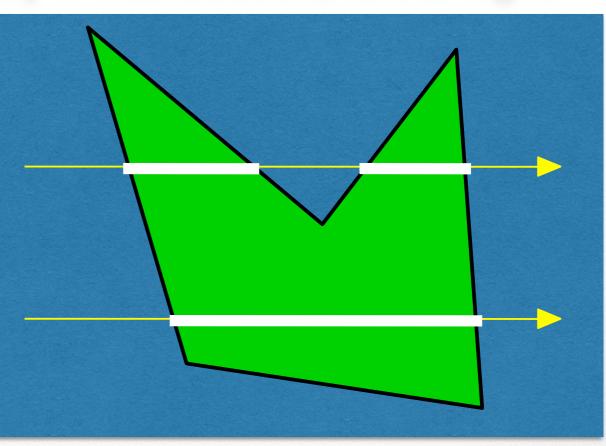
#### **Concave Polygons: Odd-Even Test**

- Approach 1: odd-even test
- For each scan line
  - Find all scan line/polygon intersections
  - Sort them left to right
  - Fill the interior spans between intersections
- Parity rule: inside after an odd number of crossings



# **Edge vs Scan Line Intersections**

- Brute force: calculate intersections explicitly
- Incremental method (Bresenham's algorithm)
- Caching intersection information
  - Edge table with edges sorted by ymin
  - Active edges, sorted by x-intersection, left to right
- Process image from smallest y<sub>min</sub> up

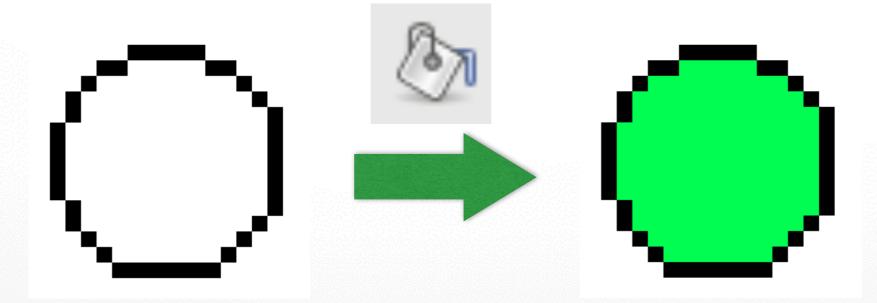


#### **Concave Polygons: Tessellation**

- Approach 2: divide non-convex, non-flat, or non-simple polygons into triangles
- OpenGL specification
  - Need accept only simple, flat, convex polygons
  - Tessellate explicitly with tessellator objects
  - Implicitly if you are lucky
- Most modern GPUs scan-convert only triangles

# **Flood Fill**

- Draw outline of polygon
- Pick color seed
- Color surrounding pixels and recurse
- Must be able to test boundary and duplication
- More appropriate for drawing than rendering

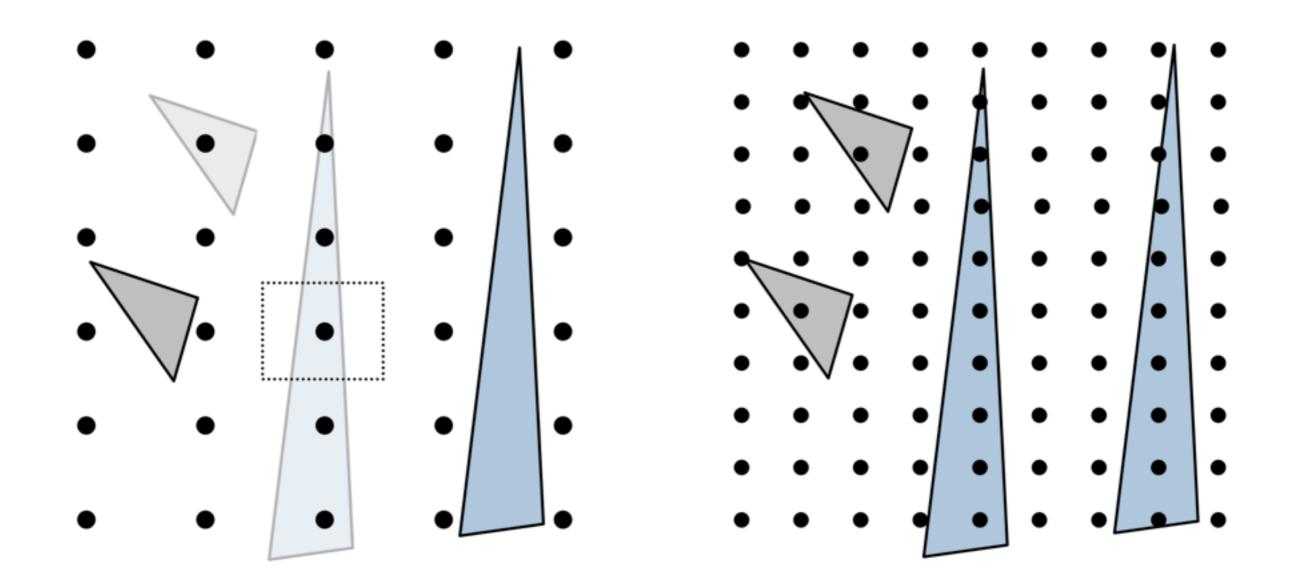


# Outline

- Scan Conversion for Lines
- Scan Conversion for Polygons
- Antialiasing

#### Aliasing

Point sampling



#### Aliasing

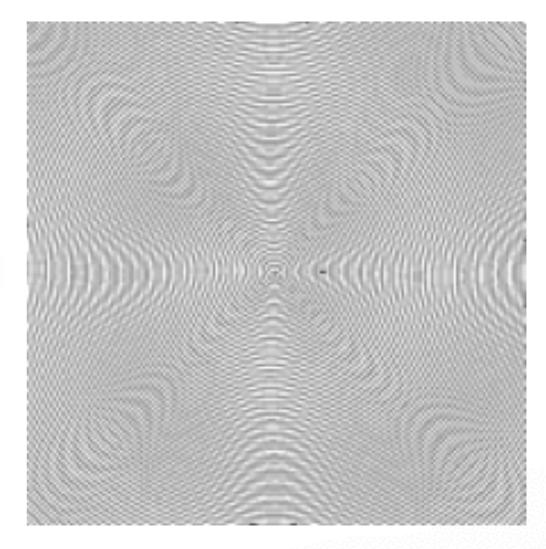
Moiré Patterns





# Aliasing

- Artifacts created during scan conversion
- Inevitable (going from continuous to discrete)
- Aliasing (name from digital signal processing): we sample a continues image at grid points
- Effect
  - Jagged edges
  - Moire patterns



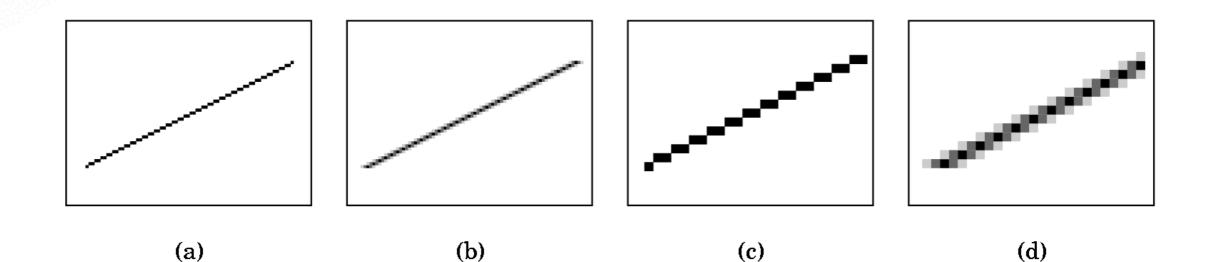
Moire pattern from sandlotscience.com

#### **More Aliasing**



#### **Antialiasing for Line Segments**

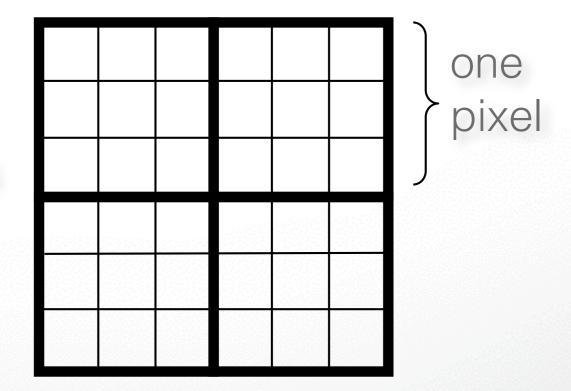
• Use area averaging at boundary



- (c) is aliased, magnified
- (d) is antialiased, magnified

# **Antialiasing by Supersampling**

- Mostly for off-line rendering (e.g., ray tracing)
- Render, say, 3x3 grid of mini-pixels
- Average results using a filter
- Can be done adaptively
  - Stop if colors are similar
  - Subdivide at discontinuities



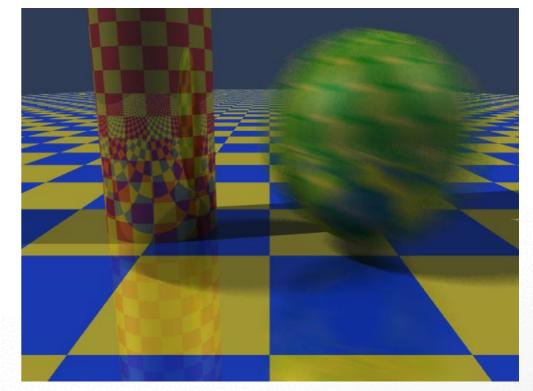
# **Supersampling Example**



- Other improvements
  - Stochastic sampling: avoid sample position repetitions
  - Stratified sampling (jittering) : perturb a regular grid of samples

## **Temporal Aliasing**

- Sampling rate is frame rate (30 Hz for video)
- Example: spokes of wagon wheel in movies
- Solution: supersample in time and average
  - Fast-moving objects are blurred
  - Happens automatically with real hardware (photo and video cameras)
    - Exposure time is important (shutter speed)
  - Effect is called motion blur



Motion blur

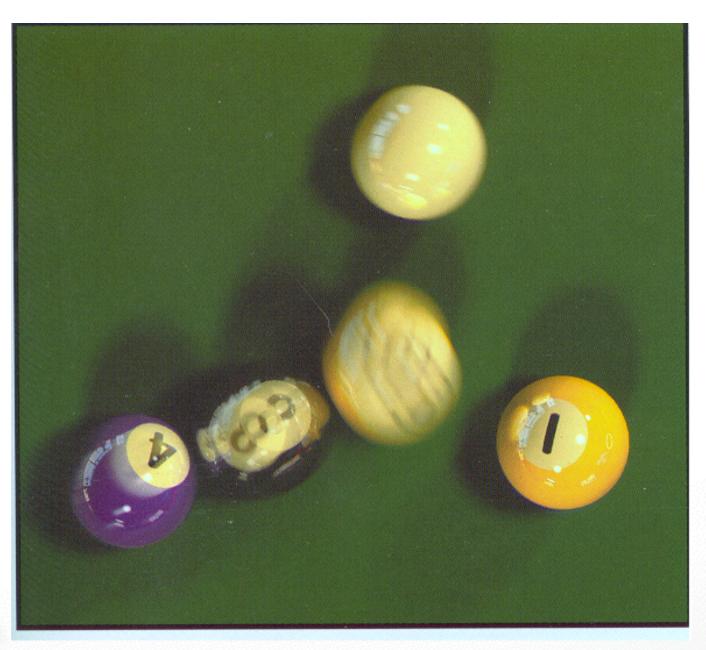
#### Wagon Wheel Effect



#### **Motion Blur Example**

Achieve by stochastic sampling in time

T. Porter, Pixar, 1984 16 samples / pixel / timestep



# Summary

- Scan Conversion for Polygons
  - Basic scan line algorithm
  - Convex vs concave
  - Odd-even rules, tessellation
- Antialiasing (spatial and temporal)
  - Area averaging
  - Supersampling
  - Stochastic sampling

#### http://cs420.hao-li.com

# Thanks!

