Fall 2014

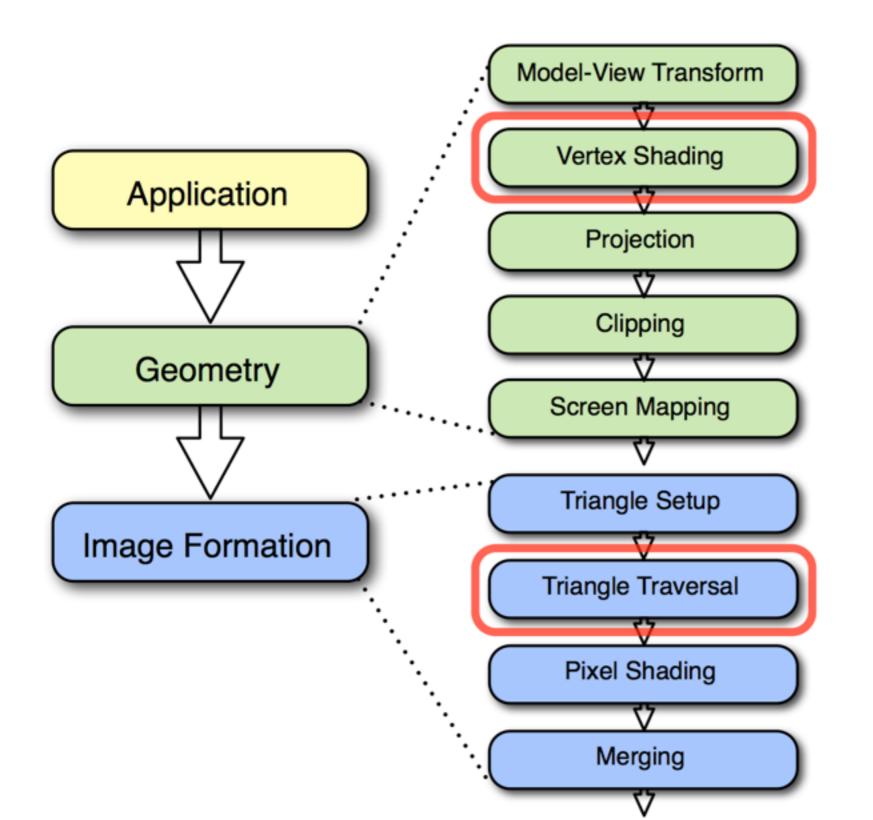
1

CSCI 420: Computer Graphics

7.1 Rasterization



Rendering Pipeline



compute vertex attributes, e.g. evaluate lighting model to compute vertex color

rasterize triangles and interpolate vertex attributes

2

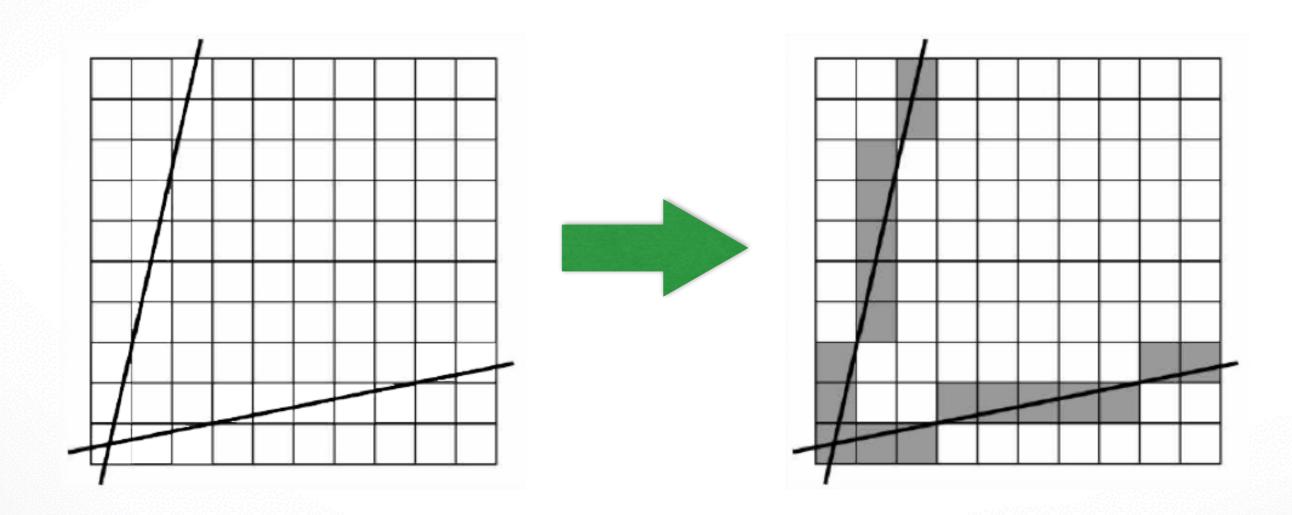
Outline

- Scan Conversion for Lines
- Scan Conversion for Polygons
- Antialiasing

Rasterization (scan conversion)

- Final step in pipeline: rasterization
- From screen coordinates (float) to pixels (int)
- Writing pixels into frame buffer
- Separate buffers:
 - depth (z-buffer),
 - display (frame buffer),
 - shadows (stencil buffer),
 - blending (accumulation buffer)

Rasterizing a line

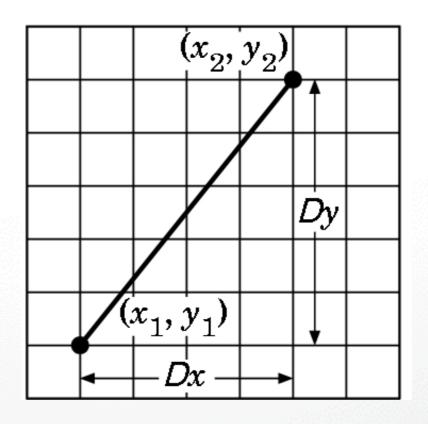


Digital Differential Analyzer (DDA)

Represent line as

$$y = mx + h$$
 where $m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{\Delta y}{\Delta x}$

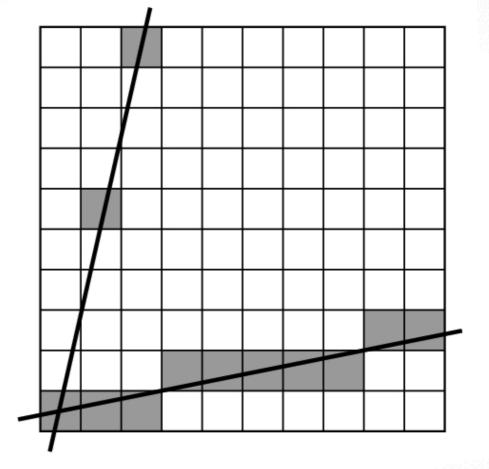
- Then, if $\Delta x = 1$ pixel, we have $\Delta y = m \ \Delta x = m$



Digital Differential Analyzer

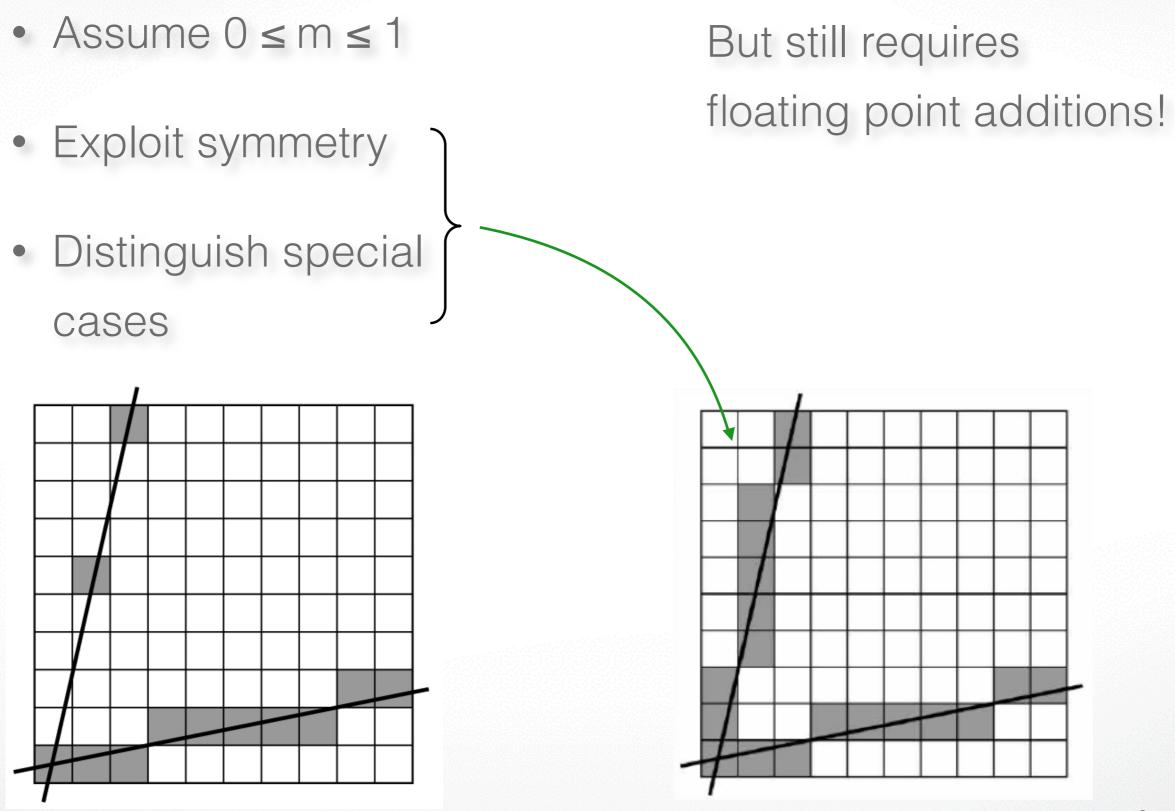
• Assume write_pixel(int x, int y, int value)

```
for (i = x1; i <= x2; i++)
{
    y += m;
    write_pixel(i, round(y), color);
}</pre>
```



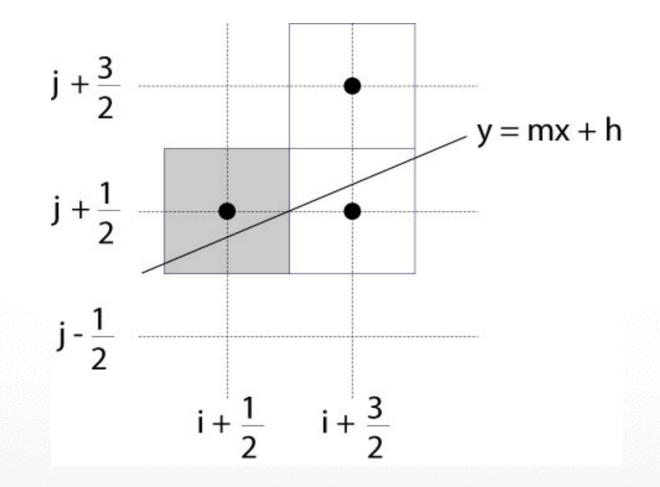
- Problems:
 - Requires floating point addition
 - Missing pixels with steep slopes: slope restriction needed

Digital Differential Analyzer (DDA)



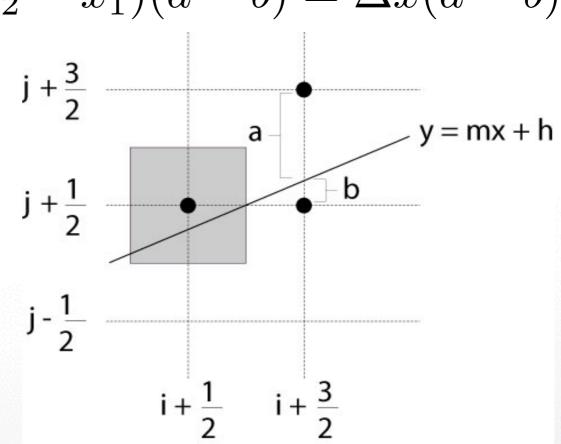
Bresenham's Algorithm I

- Eliminate floating point addition from DDA
- Assume again $0 \le m \le 1$
- Assume pixel centers halfway between integers



Bresenham's Algorithm II

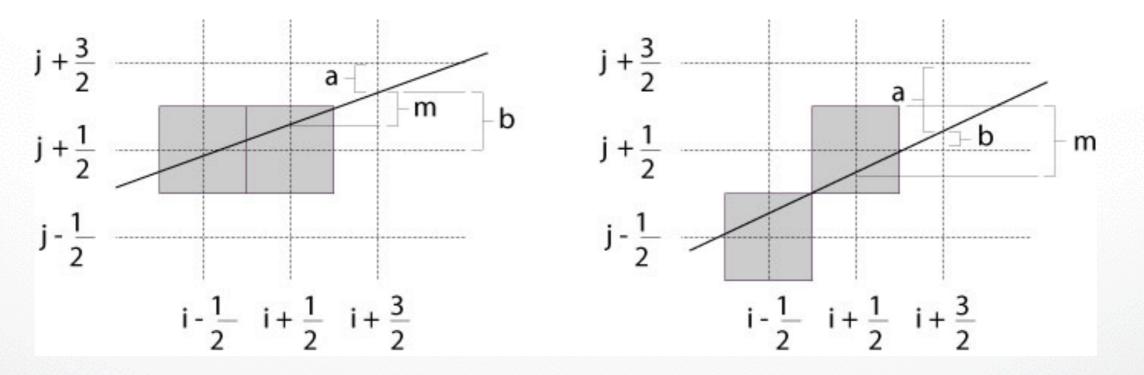
- Decision variable a b
 - If a b > 0 choose lower pixel
 - If $a b \leq 0$ choose higher pixel
- Goal: avoid explicit computation of a b
- Step 1: re-scale $d = (x_2 x_1)(a b) = \Delta x(a b)$
- d is always integer



Bresenham's Algorithm III

- Compute d at step k + 1 from d at step k!
- Case: j did not change $(d_k > 0)$ - a decreases by m, b increases by m-(a - b) decreases by $2m = 2(\frac{\Delta y}{\Delta x})$

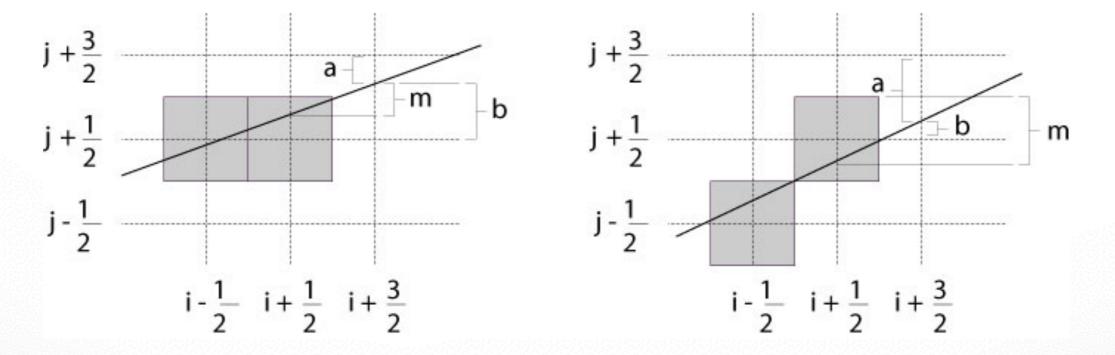
-
$$\Delta x(a-b)$$
 decreases by $2\Delta y$



Bresenham's Algorithm IV

- Case: j did change $(d_k \leq 0)$
 - $a\,\mathrm{decreases}\,\,\mathrm{by}\,m-1$, $b\,\,\mathrm{increases}\,\,\mathrm{by}\,m-1$
 - (a-b) decreases by $2m-2=2(rac{\Delta y}{\Delta x}-1)$

- $\Delta x(a-b)$ decreases by $2(\Delta y - \Delta x)$



Bresenham's Algorithm V

• So
$$d_{k+1} = d_k - 2\Delta y$$
 if $d_k > 0$

• And
$$d_{k+1} = d_k - 2(\Delta y - \Delta x)$$
 if $d_k \le 0$

• Final (efficient) implementation:

void draw_line(int x1, int y1, int x2, int y2) {
 int x, y = y0;
 int dx = 2*(x2-x1), dy = 2*(y2-y1);
 int dydx = dy-dx, D = (dy-dx)/2;

Bresenham's Algorithm VI

- Need different cases to handle m > 1
- Highly efficient
- Easy to implement in hardware and software
- Widely used

Outline

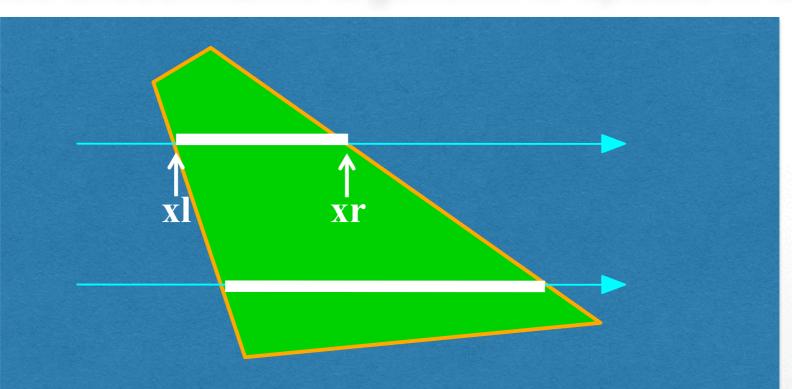
- Scan Conversion for Lines
- Scan Conversion for Polygons
- Antialiasing

Scan Conversion of Polygons

- Multiple tasks:
 - Filling polygon (inside/outside)
 - Pixel shading (color interpolation)
 - Blending (accumulation, not just writing)
 - Depth values (z-buffer hidden-surface removal)
 - Texture coordinate interpolation (texture mapping)
- Hardware efficiency is critical
- Many algorithms for filling (inside/outside)
- Much fewer that handle all tasks well

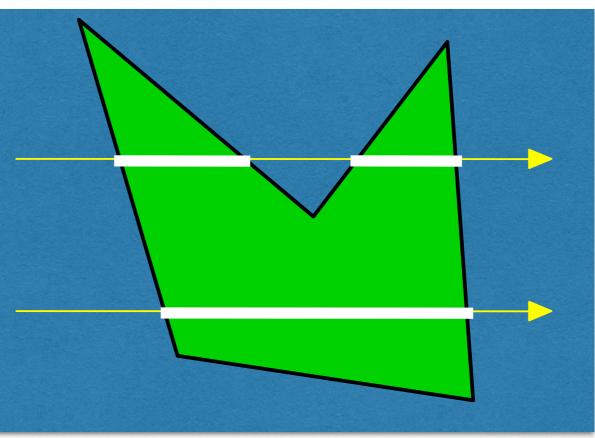
Filling Convex Polygons

- Find top and bottom vertices
- List edges along left and right sides
- For each scan line from bottom to top
 - Find left and right endpoints of span, xI and xr
 - Fill pixels between xl and xr
 - Can use Bresenham's algorithm to update xI and xr



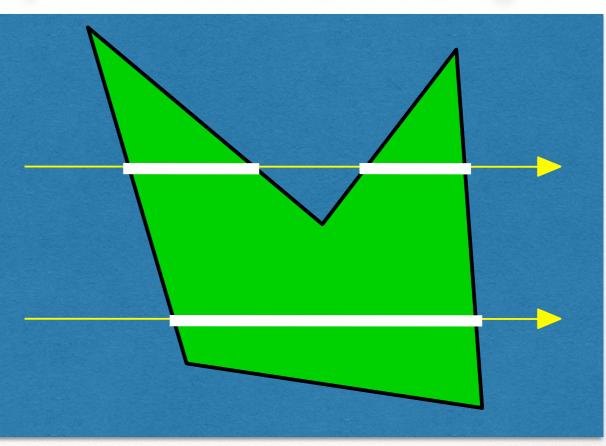
Concave Polygons: Odd-Even Test

- Approach 1: odd-even test
- For each scan line
 - Find all scan line/polygon intersections
 - Sort them left to right
 - Fill the interior spans between intersections
- Parity rule: inside after an odd number of crossings



Edge vs Scan Line Intersections

- Brute force: calculate intersections explicitly
- Incremental method (Bresenham's algorithm)
- Caching intersection information
 - Edge table with edges sorted by ymin
 - Active edges, sorted by x-intersection, left to right
- Process image from smallest y_{min} up

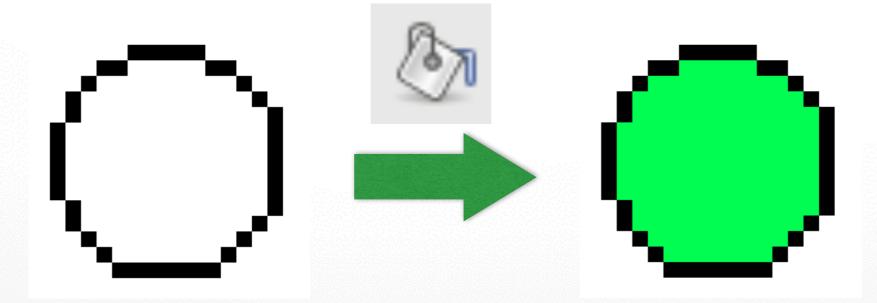


Concave Polygons: Tessellation

- Approach 2: divide non-convex, non-flat, or non-simple polygons into triangles
- OpenGL specification
 - Need accept only simple, flat, convex polygons
 - Tessellate explicitly with tessellator objects
 - Implicitly if you are lucky
- Most modern GPUs scan-convert only triangles

Flood Fill

- Draw outline of polygon
- Pick color seed
- Color surrounding pixels and recurse
- Must be able to test boundary and duplication
- More appropriate for drawing than rendering

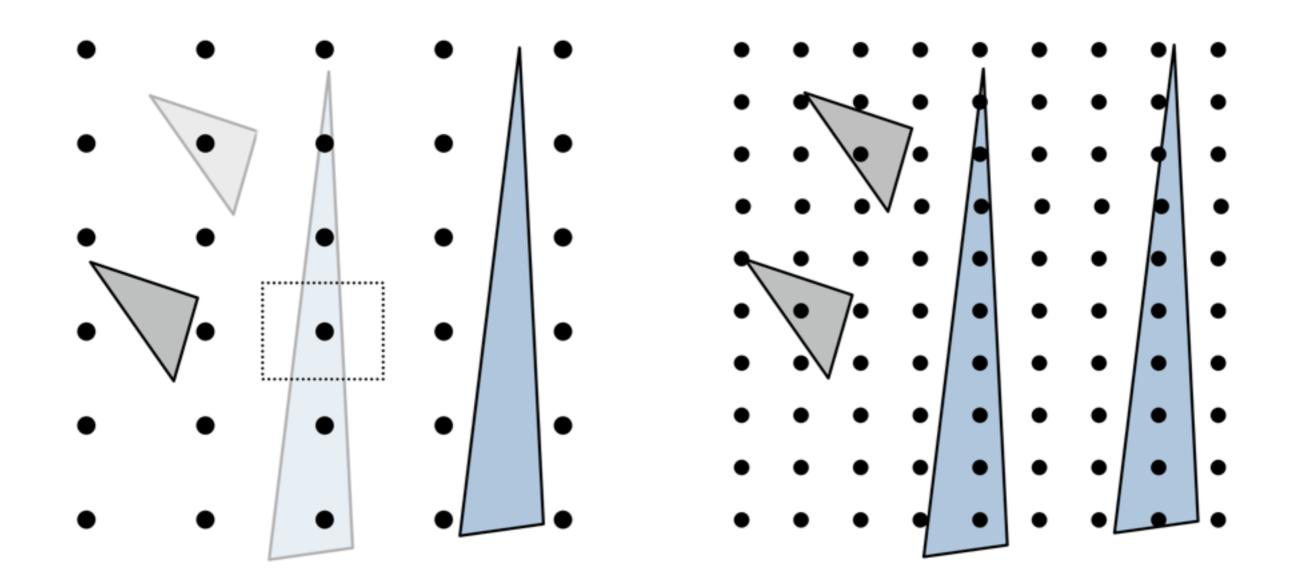


Outline

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- Scan Conversion for Polygons
- Antialiasing

Aliasing

Point sampling



Aliasing

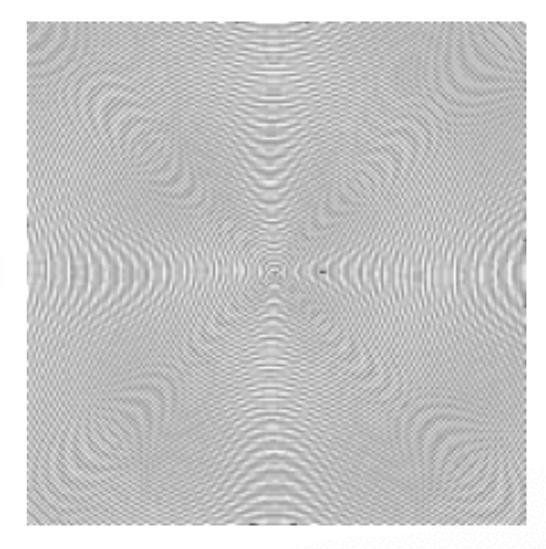
Moiré Patterns





Aliasing

- Artifacts created during scan conversion
- Inevitable (going from continuous to discrete)
- Aliasing (name from digital signal processing): we sample a continues image at grid points
- Effect
 - Jagged edges
 - Moire patterns



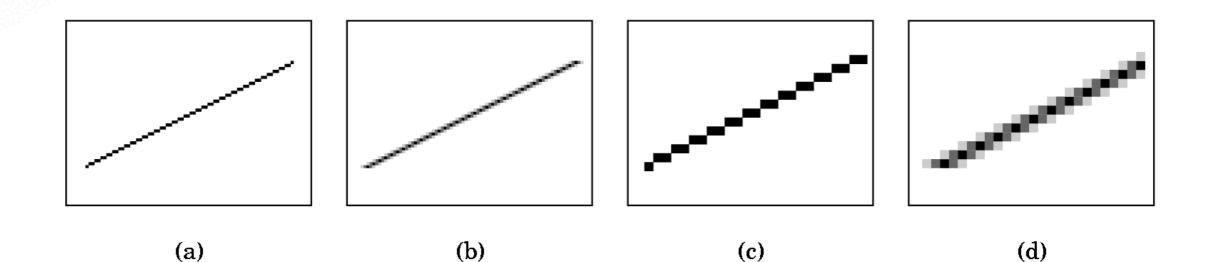
Moire pattern from sandlotscience.com

More Aliasing



Antialiasing for Line Segments

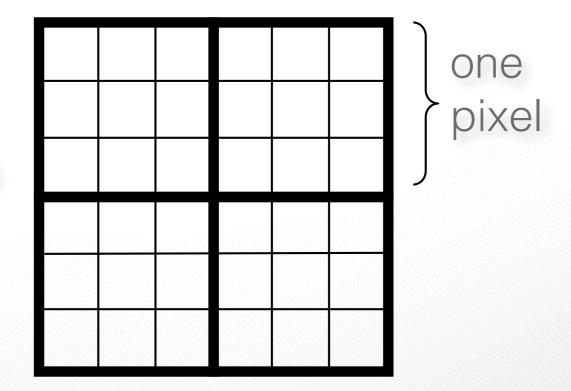
• Use area averaging at boundary



- (c) is aliased, magnified
- (d) is antialiased, magnified

Antialiasing by Supersampling

- Mostly for off-line rendering (e.g., ray tracing)
- Render, say, 3x3 grid of mini-pixels
- Average results using a filter
- Can be done adaptively
 - Stop if colors are similar
 - Subdivide at discontinuities



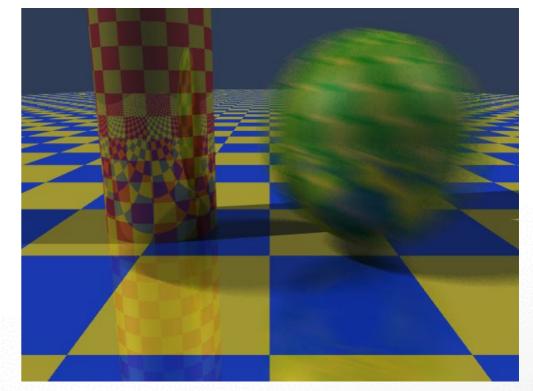
Supersampling Example



- Other improvements
 - Stochastic sampling: avoid sample position repetitions
 - Stratified sampling (jittering) : perturb a regular grid of samples

Temporal Aliasing

- Sampling rate is frame rate (30 Hz for video)
- Example: spokes of wagon wheel in movies
- Solution: supersample in time and average
 - Fast-moving objects are blurred
 - Happens automatically with real hardware (photo and video cameras)
 - Exposure time is important (shutter speed)
 - Effect is called motion blur



Motion blur

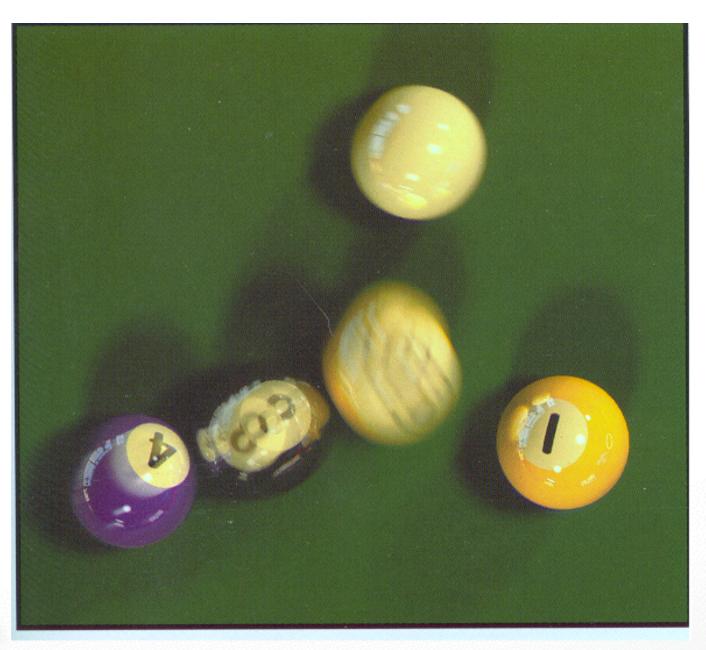
Wagon Wheel Effect



Motion Blur Example

Achieve by stochastic sampling in time

T. Porter, Pixar, 1984 16 samples / pixel / timestep



Summary

- Scan Conversion for Polygons
 - Basic scan line algorithm
 - Convex vs concave
 - Odd-even rules, tessellation
- Antialiasing (spatial and temporal)
 - Area averaging
 - Supersampling
 - Stochastic sampling

http://cs420.hao-li.com

Thanks!

